

# Evaluation of Project Duration Uncertainty using the Dependency Structure Matrix and Monte Carlo Simulations

*Evaluación de la incertidumbre en la duración de proyectos usando la Matriz de Estructura Dependiente y Simulaciones de Monte Carlo*

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## Abstract

The sequence of tasks is vital to the development of any project. The order of tasks is influenced by the information flow among them. The dependency structure matrix (DSM) can be used to model information flow. However, the information used by the DSM, including task duration, time required for communication, and task overlap, can have uncertain values. The aim of this paper is to analyze the effect of uncertainty on the scheduling of tasks using the DSM. Monte Carlo Simulation is applied to represent uncertainty in time estimates for projects using DSM. Conventional project duration, normal project duration with communication times, and normal project duration containing natural overlapping were considered for project time estimations. Several distribution functions were used to represent the uncertainty. It is concluded that project duration has normal distribution behavior that is independent of the type of input parameter distribution functions; that mean values of the input parameters give a good estimation of mean project duration; that interval and inner interval arithmetic give overestimation and underestimation of project duration times respectively.

**Keywords:** DSM, Project Duration, Managing Project, Monte Carlo Simulation, Interval Arithmetic.

## Introduction

The Dependency Structure Matrix (DSM) is a widely used tool because it allows the different parts of the project or product to be broken down or to be put together. The complexity is simplified by breaking down the project into smaller tasks, identifying the relationship between them, assessing their impact on the project, and assigning resources to individual tasks (Browning 2001). DSM has been applied to a large number of systems (Pektaş and Pultar, 2006; Cronemyr et al. 2001; Smith and Morrow 1999), including construction projects (Srou et al., 2013).

Moreover, the scheduling of projects is based on finding resources and scheduling activities with the goal of optimizing the efficiency of the project (Ponz et al., 2011). Overlapping of sequential activities occurs on most construction projects (Srou et al, 2013), which requires a two-way exchange of information among dependent design disciplines (Wang et al., 2006). The conventional tool for scheduling is the PERT/CPM, however, the PERT/CPM is not an appropriate tool for analyzing a project with overlapping because it is unable to model information flow (Wang and Lin 2009, Węglarz et al. 2011). Therefore, it cannot be used to model interdependent tasks and loops (Maheswari and Varghese, 2005).

As a result of the factors previously mentioned, recent efforts to reconcile project scheduling and DSM have sought to produce a tool that serves two purposes: analysis and project scheduling (Maheswari and Varghese, 2005). Researchers have demonstrated that DSM is a powerful tool in planning

## Resumen

La secuencia de actividades es vital para el desarrollo de cualquier proyecto. El orden de las actividades está influenciado por el flujo de información entre ellas. La matriz de la estructura de dependencias (DSM) se puede utilizar para modelar el flujo de información. Sin embargo, la información utilizada por la DSM puede tener valores inciertos. El objetivo de este trabajo es analizar el efecto de la incertidumbre sobre la programación de actividades utilizando la DSM. La simulación de Monte Carlo se aplica para representar la incertidumbre en las estimaciones de tiempo para proyectos que utilizan DSM. Para las estimaciones de duración de proyecto se consideraron la duración convencional del proyecto, la duración normal de proyecto con tiempos de comunicación, y la duración normal de proyecto con superposición natural. Las incertidumbres se representaron con varias funciones de distribución. Se concluye que la duración de proyecto presenta distribución normal que es independiente del tipo de funciones de distribución de los parámetros de entrada; valores medios de los parámetros de entrada dan una buena estimación de la duración media del proyecto; las aritméticas de intervalo e intervalos interior dan una sobreestimación y subestimación de los tiempos de duración de proyecto respectivamente.

**Palabras Claves:** DSM, Duración de Proyectos, Administración de Proyectos, Simulación de Monte Carlo, Aritmética de Intervalo.

the sequence of tasks. It depicts the interaction between the tasks, allows exchanges of information to be identified and administered (Yassine et al. 1999; Chen et al. 2003), and allows knowledge management (Tang et al. 2010). In addition, DSM has been applied to planning and scheduling tasks and to calculating critical path and assigning the "amount of effort/work undertaken" for the duration of the activity.

Recently, Srou et al. (2013) presented a methodology for scheduling the design phase of fast-tracked construction projects taking into consideration information exchange among project activities. The DSM was used to generate the shortest schedule by adapting the method proposed by Maheswari and Varghese (2005).

However, tasks in a project are subject to many unknown factors (Herroelen and Leus 2005; Perminova et al. 2007) that can lead to changes in scheduling. These uncertainty-causing factors include: tasks taking more or less time than was originally estimated, resources not being available, required materials being ready before they are scheduled to arrive, tasks being introduced or withdrawn, and weather conditions. These changes or uncertainties can cause the schedule to be delayed, increase stock, or require major work, all of which lead to higher costs than those originally planned.

For example, González et al. (2010) studied the situation of construction planning in Yucatan and found that very frequently construction firms face problems caused by delays

in completion time, prompt supply of materials, and lack of labor or machinery. Because there are many unknown factors the verification of methods used to determine scheduling has been questioned (Goldratt, 1997).

One of the limitations of the research conducted by Maheswari and Verhese is the difficulty of obtaining a firm estimate of how long each task, the communication among tasks, and the overlap of tasks will take. Gálvez et al. (2012) studied the effect of uncertainty of task programming using DSM and grey theory or interval arithmetic. Shi and Blomquist (2012) extended the DSM method proposed by Maheswari and Varghese (2005) using fuzzy numbers.

The aim of this study is to analyze the effect of uncertainty on the estimation of project duration times. Monte Carlo simulation was applied to estimate the conventional project duration time, normal project duration time with communication times, and normal project duration time with natural overlapping. Uncertainty was considered in the task duration times, communication times, and time factor (for natural overlapping) using uniform, normal, and triangular distribution functions.

The remaining sections of this paper will be organized in the following manner. The second section provides brief descriptions of five important topics related to this paper, namely DSM, task planning under uncertainty, Monte Carlo simulation, interval arithmetic, and the estimation of project duration. The third section describes the Monte Carlo numerical experiment that was conducted and analyzes the results. Additionally, the applications of interval arithmetic (standard and inner) are compared with the values obtained by the Monte Carlo simulation. The fourth section provides conclusions.

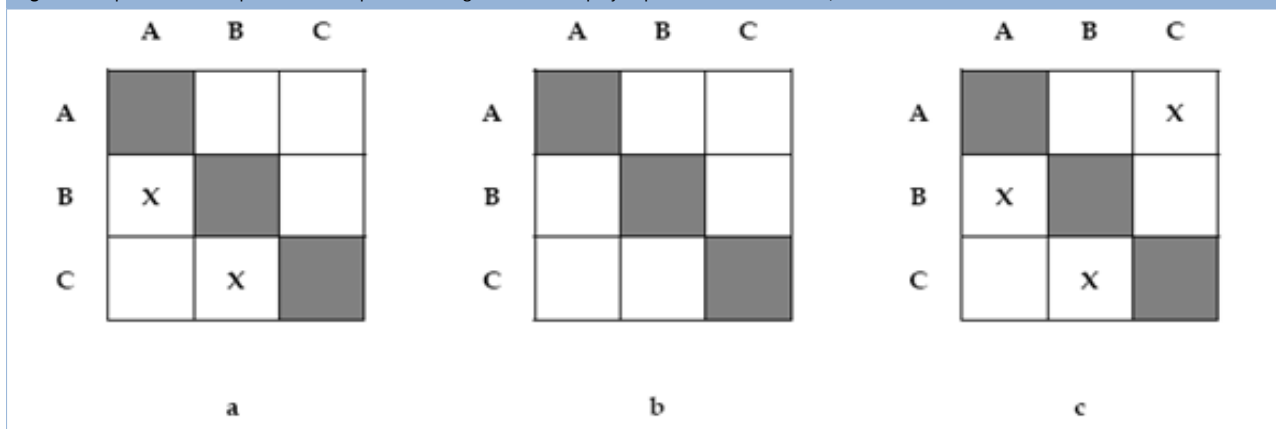
This section provides brief descriptions of DSM, task planning under uncertainty, Monte Carlo simulation, interval arithmetic, and the estimation of project duration.

DSM shows the relationship between the components of a system in a format that facilitates visual analysis. DSM is a square matrix that has the same number of rows as columns. The elements that lie outside the diagonal signify the dependence of one element upon the others. The content of the columns can be understood as "information given to" and by row as "information received from". In other words, the entries can be seen by reading the columns, and the dependent factors can be seen by reading the rows (Browning 2001).

Examined from the point of view of task scheduling, there are 3 types of configurations (see figure 1): parallel, sequential, or coupled. When tasks are parallel, they do not interact with each other. For example, tasks A, B, and C in figure 1b do not require any exchange of information; whereas in figure 1a, when the tasks are sequential, one information element of task A influences the behavior of or decisions made concerning the other task B in a single direction. Consequently, the parameters of task C are selected on the basis of B, and B on the basis of A. If tasks are coupled, the flow of information is related, due to the fact that element C influences A or vice versa (A influences B, and B influences C), as shown in figure 1c. DSM can also represent tasks which are interrelated (Eppinger et al. 2010).

The process of organizing the order of tasks can be achieved by moving a column left or right or a row up or down with the aim of obtaining a matrix that does not have marks over the diagonal cells or marks near the diagonal cells. This is known as partitioning.

Figure 1. Graphic and DSM representation of possible configurations in the project process. Self Elaboration, 2014



The literature on the scheduling of projects focuses on the generation of tangible tasks that allow the objective to be optimized, usually within the project's duration. This scheduling is used as a basis for planning or programming and fulfills a number of important functions (Aytug et al. 2005). These functions include locating the resources for different tasks, coordinating tasks with outside organizations, having a communication base, and allowing for agreements and sub-contracting. However, as previously mentioned, there are a number of uncertain factors that make scheduling projects difficult.

In general, there are five different ways of approaching uncertain factors when scheduling projects (Herroelen and

Leus, 2005): reactive scheduling, stochastic scheduling, fuzzy scheduling, proactive (robust) scheduling, and sensitivity analysis. Reactive scheduling does not attempt to incorporate uncertainty into the base planning, but rather revises and re-optimizes the original scheduling when an unexpected event takes place (Vieira et al. 2003; Sabuncuoglu and Bayiz, 2000).

Stochastic scheduling focuses on tasks with uncertain durations with the aim of minimizing the expected length of time that a project will take, while also taking into account restrictions on resources and tasks with random lengths. This method does not use a base plan and requires significant computer effort. The programming of fuzzy tasks indicates

that the probability distribution of a task's duration is unknown due to a lack of historical data. For this reason, the length of time is usually estimated by human resources experts whose judgments can be imprecise. As a result, instead of probable distributions, member functions based on fuzzy sets are used, and these member functions translate into start and finish times of fuzzy tasks (Slowinski and Hapke, 2000). Another method is to represent human experts as normally distributed variables (such as Cox, 1995), but allow task durations to have other continuous distributions, such as triangular or uniform distributions (Lee, 2005).

Monte Carlo simulation involves sampling the model using the parameters' probability distribution functions, such as normal or uniform, to provide parameter values. Usually, a random number is used to obtain a value based on the parameters of the distribution function. When a value for each parameter has been calculated, the model is quantified to obtain an answer. This answer is then placed into a frequency table. The entire calculation process is then repeated until the desired number of iterations is reached.

In addition to the Monte Carlo simulation, we explore the use of interval arithmetic to estimate the range of project duration times. Standard interval arithmetic and inner interval arithmetic will be compared with the maximum and minimum values given by Monte Carlo simulation.

Standard interval arithmetic operates with real intervals

$$[x_1, x_2] = \{x \in R | x_1 \leq x \leq x_2\} \quad [1]$$

where  $x_1$  and  $x_2$  are real numbers. For any real arithmetic operation  $\{x \text{ op } y\}$ , the corresponding interval arithmetic operation  $\{X \text{ op } Y\}$  is defined where the result is an interval containing every possible number produced by  $\{x \text{ op } y\}, x \in X, y \in Y$ . The standard interval arithmetic operations needed here are (in our applications, all the numbers are positive numbers) [2],[3],[4].

$$X + Y = [(x_1 + y_1), (x_2 + y_2)] \quad [2]$$

$$X - Y = [(x_1 - y_2), (x_2 - y_1)] \quad [3]$$

$$X * Y = [x_1 y_1, x_2 y_2] \quad [4]$$

$$X + Y = [\min((x_1 + y_2), (x_2 + y_1)), \max((x_1 + y_2), (x_2 + y_1))] \quad [5]$$

$$X - Y = [\min((x_1 - y_1), (x_2 - y_2)), \max((x_1 - y_1), (x_2 - y_2))] \quad [6]$$

With these equations the full range of possible function values in the defined region are always included. A disadvantage of standard interval arithmetic is the dependency problem: when a given variable occurs more than once in interval computation it is treated as a different variable at each occurrence. Inner interval arithmetic assumes that all operands are dependent. The inner interval operations needed here are (see Zilinskas and Bogle, 2004). [5], [6], [7]

However, the estimates obtained for a range of function values using inner interval arithmetic are not guaranteed to be enclosed in the function's range, and therefore, will not

cover the entire range. Finally, conventional times for the duration of a project, normal duration of a project with time for communication, and normal duration of a project with natural overlaps are briefly explained. Conventional time (CT) only take into account the length of time required to carry out tasks, and can be determined using DSM in the following manner. [8], [9], [10]

$$X * Y = [\max(x_1 * y_2, x_2 * y_1), \min(x_1 * y_1, x_2 * y_2)] \quad [7]$$

$$(EF)_i = (ES)_i + A_{ii} \quad 0 < i \leq n \quad [8]$$

$$(ES)_j = \text{Max}[(EF)_i] \quad 0 < i \leq n, 0 < j \leq n \quad [9]$$

$$P = \text{Max}[(EF)_j] \quad 0 < j \leq n \quad [10]$$

$$(ES)_j = \text{Max}[(EF)_i + A_{ji}] \quad 0 < i \leq n, 0 < j \leq n \quad [11]$$

Where  $P$  is the conventional project duration,  $A_{ii}$  represents the time of duration for task  $i$ . Additionally,  $n$  refers to the number of tasks;  $i$  refers to all previous tasks (intermediary tasks) of  $j$ ;  $j$  refers to the currently selected task identified by the partitioned DSM matrix. ES refers to Early Start and EF refers to Early Finish.

Normal time (NT) for project duration is the duration of the project, including the times for the duration of each task as well as the time for communication. Maheswari and Varghese (2005) have determined the normal time for the duration of a project with DSM using the communication times that occur between tasks and their duration. Communication time is the time spent obtaining information before or after completing a task, as well as time spent in meetings, organizing those meetings, sending and receiving emails, and other duties. The NT can be determined using Eqs. [8] and [10] and changing Eq. [9] for the following equation (for more details see Maheswari and Varghese, 2005). [11]

Where the elements outside the diagonal,  $A_{ji}$  are equivalent to the communication times of each task. The meanings of  $n$ ,  $i$ , and  $j$  are the same as previously stated. When one task depends on another, there are two possibilities: they may overlap, or they may not. Situations in which there is no overlap are of interest to administrators and carry a comparative minimum of risk. In situations where there is overlap, the upstream task may communicate available preliminary information to the downstream task and enable the downstream task to begin earlier (Wang and Lin 2009).

The relationship from Finish to Start (FS) is a conventional representation of the relationship between tasks in DSM, which by itself does not completely represent the overlap of projects. It is also possible to estimate the duration of overlap by taking into account the time taken to transfer information between tasks through a relationship Start to Start (SS).

In the case of tasks that do not overlap, it is assumed that the following, or successor, task will not start until the previous task or tasks have been completed. Tasks that overlap assume that a successor task can start before receiving information about tasks that took place previously and that these tasks are able to provide information before they have been finalized.

The times that allow for overlap are represented by the time factor, which is defined as the ratio between the time taken to exchange information and the time taken to carry out a task (Maheswari and Varghese, 2005). These times are represented by the factors  $T_p$  and  $T_s$ , where  $T_p$  represents the time factor to send information from a previous task, and  $T_s$  is the time factor required to receive information for the successor task.

$$(EF)_j = (ES)_j + B_{jj} \quad 0 < j \leq n \quad [12]$$

$$(ES)_j = \text{Max}[(ES)_i + (B_{ji} \times B_{ii}) - (C_{ji} \times C_{jj})] \quad 0 < i \leq n, 0 < j \leq n \quad [13]$$

To determine the time for the duration of a project with overlapping tasks (NTO), the Eq. [10] can be used, but replacing Eqs. [8] and [9] by Eqs. [12] and [13]. Where  $B_{ji}$  and  $C_{ji}$  are two matrices representing time factors,  $B_{ji}$  represents all the values of  $T_p$ , and represents  $C_{ji}$  all the values of  $T_s$ . The significance of the remaining elements is the same as previously indicated.

## Monte Carlo Numerical Experiments

### Description of the case study

This section presents the procedure for solving the conventional time for the duration of a project, the normal time for the duration of a project including the time for communication, and the normal time for project duration when the project has overlapping tasks. To provide a clearer understanding, this solution procedure is applied to a modified version of an example given by Maheswari and Varghese (2005), but including uncertainty in task duration, communication times, and time factors. This example consists of 10 tasks (A through J), as shown in table 1. Information is also provided about the previous tasks, the mean duration times, and standard deviations.

Table 2 presents the mean and standard deviation of communication times and the values of the matrices B and C, where  $B_{ji}$  represents the values of  $T_p$  (information required prior to carrying out the task). For example, 0.78 in  $B_{CA}$  implies that A can send the required information through C at the end of 0.78 times its duration.  $C_{ji}$  represents the values of  $T_s$  (time factor for receiving information). For example, 0.095 in  $C_{DA}$  implies that it is essential that to continue, D receive information from A, but only at 0.095 of the time of its duration, instead of at the beginning of the task.

For the calculation of the conventional project duration, the normal project duration with communication times, the normal overlap project duration, probability distribution functions of task duration are needed. Therefore, communication times and time factor values were sampled from normal, uniform, and triangular distribution functions. Figure 2 provides an example of the distribution function of task A duration time.

**Table 1:** List of tasks in the example with the mean duration time ( $A_{ij}$ ) and standard deviation for each task. Self Elaboration, 2014

Task Identification	Previous Information	Mean Duration (Days)	Standard Deviation
A	-	5.9	0.1
B	D	8.2	0.45
C	A	6.85	0.33
D	A, F	3.9	0.05
E	B	8.85	0.28
F	A, C	1.0	0.0
G	F, J	2.05	0.03
H	I	10.05	0.325
I	D, G, E	4.95	0.225
J	F, B	3.0	0.0

**Table 2:** The mean and standard deviations for communication times ( $A_{ij}$ ) between tasks, time factors  $T_p$  ( $B_{ji}$ ), and time factors  $T_s$  ( $C_{ji}$ ). Self Elaboration, 2014

j	i	Communication mean time (Days), $A_{ij}$		Time Factors $T_p$ , $B_{ji}$		Time Factors $T_s$ , $C_{ji}$	
		mean	Standard Deviation	mean	Standard Deviation	mean	Standard Deviation
C	A	1.00	0.0	0.78	0.01	0.10	0.0
F	C	1.90	0.05	0.585	0.008	0.310	0.0050
D	A	0.80	0.0	0.795	0.003	0.095	0.0025
D	F	0.30	0.0	0.685	0.007	0.200	0.0050
B	D	4.05	0.18	0.885	0.008	0.375	0.0125
J	F	1.50	0.0	0.895	0.003	0.195	0.0075
J	B	0.0	0.0	0.960	0.020	0.0	0.0
G	F	0.10	0.0	0.480	0.010	0.480	0.010
G	J	0.40	0.0	0.980	0.010	0.310	0.005
E	B	4.25	0.125	0.865	0.018	0.100	0.0
I	D	3.45	0.075	0.580	0.010	0.195	0.0075
I	G	2.00	0.05	0.795	0.003	0.560	0.0350
I	E	3.05	0.175	0.980	0.010	0.0	0.0
H	I	4.90	0.150	0.665	0.018	0.405	0.0125

## Results

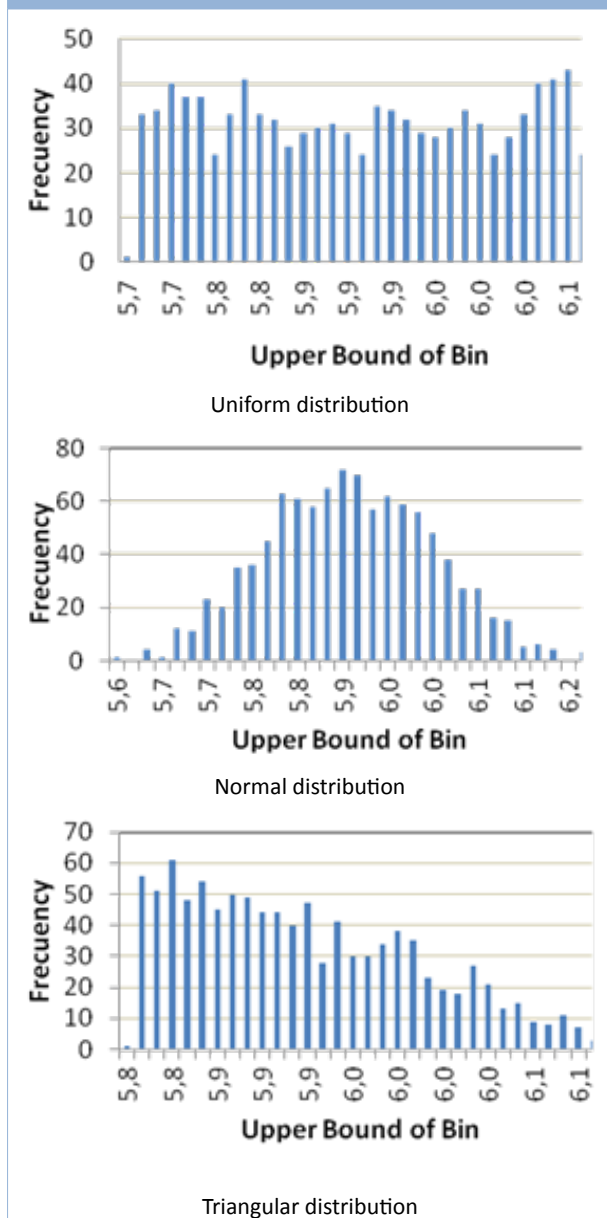
Values of task duration, communication times, and time factors were generated randomly from the probability distribution functions. Then using equations 1 to 12, values of conventional project duration, normal project duration with communication times, and normal overlap project duration were calculated, respectively. These values were placed in a frequency table, 1000 calculations were completed, and the data from this table were analyzed. MS Excel was used in all computations. Histograms and descriptive statistics were constructed for each type of project duration time and distribution function.

The conventional project duration results are given in table 3. All distribution functions gave similar results. From the values of kurtosis and skewness, it is clear that the conventional project duration has a normal distribution. This result is the same whether the input data have a uniform, normal, or triangular distribution.

The mean and median of a conventional project are also similar because the distribution is normal. If the mean values of each duration task are used to calculate the conventional

project duration, a value of 49.70 is obtained, which is close to the mean values obtained in the Monte Carlo simulations. If the minimum and maximum values of each task duration are used to calculate the conventional project duration using standard interval arithmetic, values of 46.20 and 53.20 are obtained, which are overestimations of the values obtained in the Monte Carlo simulations. On the other hand, if inner interval arithmetic is used, values of 49.50 and 49.90 are obtained, which are underestimations of the values obtained in the Monte Carlo simulations.

**Figure 2.** Task A distribution functions included in the Monte Carlo simulation. Self Elaboration, 2014.



The normal project duration and normal overlap project duration results are also given in table 3. If the mean values of each task duration and communication time are used to calculate the normal project duration and normal overlap project duration, values of 69.15 and 32.05 are obtained respectively, which is near the mean values obtained in the Monte Carlo simulations. If the minimum and maximum values of each task duration are used to calculate the normal project duration and normal overlap project duration, using standard interval arithmetic, values of [64.3 and 74.0] and [29.48 and 34.68] are obtained respectively, which are overestimations of the values obtained in the Monte Carlo simulations (see

table 3). On the other hand, if inner interval arithmetic is used, values of [68.70 and 69.60] and [30.96 and 32.83] are obtained, which are underestimations of the values obtained in the Monte Carlo simulations.

**Table 3.** Project duration for uniform, normal and triangular input distribution functions. (SD=standard deviation). Self Elaboration, 2014.

	Input Distribution Function		
	Uniform	Normal	Triangular
Conventional project duration			
Mean	49.412	49.666	49.873
Median	49.425	49.647	49.853
SD	0.782	0.763	0.527
Kurtosis	-0.286	0.096	-0.043
Skewness	-0.013	-0.015	0.142
Minimum	47.031	47.024	48.346
Maximum	51.856	52.067	51.730
Normal project duration with communication times			
Mean	68.869	69.108	69.404
Median	68.901	69.108	69.387
SD	0.871	0.812	0.571
Kurtosis	-0.151	0.193	-0.043
Skewness	-0.070	-0.049	0.119
Minimum	66.084	66.472	67.701
Maximum	71.419	71.884	71.520
Normal overlap project duration			
Mean	31.871	32.028	32.048
Median	31.873	32.033	32.045
SD	0.485	0.543	0.493
Kurtosis	-0.338	0.030	0.034
Skewness	0.008	0.006	0.059
Minimum	30.508	30.187	30.322
Maximum	33.198	33.766	33.530

Figures 3 shows distribution functions of normal overlap project duration when uniform, normal and triangular distributions are used as input distribution functions for the task duration, communication times and time factors. It may be observed that normal distribution functions are obtained independently of the kind of input distribution functions used. Similar results are observed for the distribution function of conventional project duration and normal project duration.

Table 4 reports the interval values of the project duration. The values under the column heading "Monte Carlo Simulation" are the minimum and maximum values, including normal, uniform, and triangular distributions. Overestimations are obtained using standard interval arithmetic, whereas underestimations are obtained if inner interval arithmetic is used. The last column of Table 4 gives the average values of standard and inner interval arithmetic, which are better estimations of the minimum and maximum project duration times.

Monte Carlo simulations were performed using uniform and normal distributions for the input parameter, with standard distribution value equal to two times the values of the previous simulations. The results are given in table 5, columns headed "SD" represent the Monte Carlo simulation performed with a standard deviation equal to the values given in the previous simulations, and columns headed "2SD" represent the Monte Carlo simulation performed with a standard deviation equal to two times the values in the previous simulations. The mean





**Table 4.** Interval values of project duration. Self Elaboration, 2014

Project Duration	Monte Carlo Simulation	Standard Interval Arithmetic	Inner Interval Arithmetic	Average value of Interval Arithmetic
Conventional time	47.02-52.07	46.20-53.20	49.50-49.90	47.85-51.55
Normal with communication times	66.08-71.88	64.30-74.00	68.70-69.60	66.50-71.80
Normal time with overlapping	30.19-33.77	29.48-34.68	30.96-32.83	30.22-33.76

**Table 5.** Project duration with different values of standard distribution. Self Elaboration, 2014

	Distribution function			
	Uniform		Normal	
	SD	2SD	SD	2SD
Conventional project duration				
Mean	49.412	49.663	49.666	49.718
Median	49.425	49.617	49.647	49.652
Standard deviation	0.782	1.681	0.763	1.541
Kurtosis	-0.286	0.406	0.096	0.390
Skewness	-0.013	0.091	-0.015	0.096
Minimum	47.031	45.173	47.024	42.705
Maximum	51.856	54.973	52.067	55.113
Normal project duration with communication times				
Mean	68.869	69.123	69.108	69.175
Median	68.901	69.142	69.108	69.148
Standard deviation	0.871	1.820	0.812	1.693
Kurtosis	-0.151	0.312	0.193	0.496
Skewness	-0.070	0.029	-0.049	0.069
Minimum	66.084	64.043	66.472	60.856
Maximum	71.419	75.220	71.884	75.737
Normal overlap project duration				
Mean	31.871	31.885	32.028	32.012
Median	31.873	31.870	32.033	32.028
Standard deviation	0.485	0.783	0.543	0.952
Kurtosis	-0.338	0.245	0.030	0.244
Skewness	0.008	0.080	0.006	0.057
Minimum	30.508	29.788	30.187	28.518
Maximum	33.198	34.231	33.766	35.925

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